

| Vector functions  |   |
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| Function signature  | Description   |
| <code>vector = row_vector = create_vector</code><br><code>vector(X), vector(K,X)</code><br><code>col_vector(X) = vector(X,'c'), col_vector(K, X) = vector(K,X,'c')</code><br><code>vec(x,K)</code><br><code>vec(x)</code> | The function <code>vector(X)</code> transforms a list <code>X</code> to a Vector. If a field or ring <code>K</code> is supplied as a the first parameter, the elements of <code>X</code> are pushed to elements of it. The parameter ' <code>c</code> ' is to indicate that the constructed vector be a column vector.  |
| <code>eps(n,j)</code><br><code>eps(m,n,j,k)</code>  | It returns <code>vector(K,x)</code> . By default <code>K = Zn(2)</code>   |
| <code>vector_append(x,a)</code><br><code>error_vector(n,E)</code>   | If <code>n</code> is a positive integer and $0 \leq j < n$ , <code>eps(n,j)</code> is the length <code>n</code> list whose $j$ -th entry is 1 and all other entries are 0. If $j$ is out of the indicated range, <code>eps(n,j)</code> is the length <code>n</code> list whose entries are all 0. Similarly, given positive integers <code>m</code> and <code>n</code> , and integers <code>j</code> and <code>k</code> such that $0 \leq j < m$ and $0 \leq k < n$ , <code>eps(m,n,j,k)</code> creates an $m \times n$ matrix with all entries 0 except 1 in the $(j,k)$ entry. If either $j$ or $k$ is not in the stated range, the call returns the $m \times n$ null matrix.<br>Examples:<br><code>eps(4,1) ⇒ [0, 1, 0, 0]</code><br><code>eps(3,4,2,2) ⇒</code><br>$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} :: \text{Matrix}[ZZ]$  |
| <code>wt(x)</code><br><code>hd(x,y)</code>  | If <code>x</code> is a vector, this function is equivalent to <code>vector(list(X)+[a])</code>  |
| <code>cyclic_shift(x)</code><br><code>cyclic_shifts(x)</code>   | If <code>E</code> is a list of pairs $(j,v)$ , $j$ in $0..n-1$ , it creates a lenght <code>n</code> vector with values <code>v</code> at the positions <code>j</code> .   |
| <code>reverse(x)</code><br><code>support(x)</code><br><code>pattern(x)</code><br><code>histogram(x)</code>  | If <code>x</code> is a list or vector, <code>wt(x)</code> is equivalent to <code>len(support(x))</code> . If <code>y</code> is another list or vector of the same length as <code>x</code> , <code>hd(x,y)</code> supplies the Hamming distance between <code>x</code> and <code>y</code> , which by definition is the cardinal of the set of indices <code>j</code> in the range of the lists/vectors such that $x_j \neq y_j$ . If both <code>x</code> and <code>y</code> are vectors, it is equivalent to <code>wt(x-y)</code> .<br>Given <code>x</code> a vector $[x_1 \dots x_n]$ , <code>cyclic_shift(x)</code> returns $[x_n, x_1 \dots x_{n-1}]$ . <code>cyclic_shifts(x)</code> return a list with all the different cycles of <code>x</code> .<br>If <code>x = [x_1, \dots, x_n]</code> is a list or a vector, it return the reverse element $x' = [x_n, \dots, x_1]$   |
| <code>convolution(a,b,k)</code><br><code>convolution(a,b)</code>  | If <code>x</code> is a list or vector, <code>support(x)</code> yields the list of the indices <code>i</code> in the range of <code>x</code> such that $x_i \neq 0$ . The function <code>pattern(x)</code> and <code>histogram</code> returns a pair $(s,v)$ , with <code>s = support(x)</code> and <code>v = vector([x[j] for j in s])</code>   |
| <code>geometric_series (x, n, s0)</code><br><code>geometric_series (x, n)</code>  | If <code>a</code> and <code>b</code> are vectors or lists and <code>k</code> is an integer, this function returns the <code>k</code> -th coefficient of the convolution of <code>a</code> and <code>b</code> , namely the sum of the terms $a_j \cdot b_{k-j}$ for $j = 0, \dots, k$ , with the conention that $a_j = 0$ if $j \geq \text{len}(a)$ and $b_{k-j} = 0$ if $k-j \geq \text{len}(b)$ . Thus <code>convolution(a,b,k) = 0</code> if $k < 0$ or $k \geq \text{len}(a) + \text{len}(b)$ . If <code>a</code> and <code>b</code> are lists, <code>convolution(a,b)</code> is the list $[\text{convolution}(a,b,k) \text{ for } k \text{ in range}(n)]$ , where $n = \text{len}(a) + \text{len}(b) - 1$ . For vectors, <code>convolution(a,b)</code> is equivalent to <code>vector(convolution(list(a),list(b)))</code> .<br>The first call produces the vector $[s_0, s_0 \cdot x, \dots, s_0 \cdot x^{(n-1)}]$ . The second is defined as <code>geometric_series(x,n,1)</code> , which therefore supplies the vector $[1, x, \dots, x^{(n-1)}]$ . |

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| flip(x)<br>flip(x,k)                                | <p>The first form transforms a list or a vector x into the list or vector whose components are <math>1-x[j]</math>, <math>j</math> in the range of x. For a binary list or vector, it concides with the result of swaping 0 and 1 (this explains the name given to the function). In the second form, k may be an index in the range of x, or a list/tuple/set of such indices and only the kth component, or the components with index in k, undergo the trasformation <math>1-x[j]</math>.</p> <p>Examples:</p> <pre> x = rd_vector(Zn(2),7) ⇒ [1, 0, 0, 1, 0, 0, 1] :: Vector[Z2] flip(x) ⇒ [1, 0, 1, 1, 0, 0, 1] :: Vector[Z2] flip(x) ⇒ [1, 0, 0, 1, 0, 0, 1] :: Vector[Z2] R = vector(Zn(5), list(range(9))) ⇒ [0,1,2,3,4,0,1,2,3] :: Vector(Z5) flip(R,(1,6)) ⇒ [0, 0, 2, 3, 4, 0, 0, 2, 3] :: Vector[Z5] flip(R) ⇒ [1, 1, 4, 3, 2, 1, 1, 4, 3] :: Vector[Z5] </pre> |
| invert_entries (a)                                  | If a is a vector with no zero entries, it returns the vector $[1/a_1, \dots, 1/a_n]$ .  |
| prod (x, y)<br>dot (x, y)                           | If x and y are lists or vectors of the same length n, prod(x, y) constructs the vector $[x_1 \cdot y_1, \dots, x_n \cdot y_n]$ and dot(x, y) yields the sum $x_1 \cdot y_1 + \dots + x_n \cdot y_n$   |
| rd_vector(K,n)                                      | Given a domain K and a integer n, it returns a vector of n elements in K.   |
| rd_nonzero_vector(K,n)                              | Given a domain K and a integer n, it returns a vector of n elements in K with not all elements equal to zero.   |
| null_vector()<br>null_vector(K)                     | It returns a vector of length 0. If a domain K is given, the null vector will have domain K.  |
| subs_element(A,x,y)                                 | Given a vector or matrix A, it changes all the entries equal to x by the element y.   |
| rd_error_vector (K, n, s)<br>rd_error_vector (K, s) | If n and s are positive integers, $s \leq n$ , and K is a field (or a ring), rd_error_vector(K, n, s) produces a vector in $K^n$ of weight s whose non-zero positions and the corresponding values have been chosen randomly. The function rd_error_vector(K, s) is defined as rd_error_vector(K, q-1, s), where q is the cardinal of K.  |
| bin_(x)   | Given a list or a vector x, it returns a vector v equal to x changing the -1 elements by 0.   |
| unbin_(x)   | Given a list or a vector x, it returns a vector v equal to x changing the 0 elements by -1.   |
| is_vector(v)  | It returns if v is of type vector.  |
| vector_resultant(v,w)                               | Given two vectors, it returns the resultant of the two vectors.   |
| append_vector(*V)                                   | Given a list of vectors it concatenates all the elements.   |