

ICCA11

Ghent University

Waldyr Alves Rodrigues Jr.:
Sketches on his Life and Work

S. Xambó & C. Lavor

UPC & Unicamp

9 August 2017

AGACSE 2015



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1. Lavor	5. Mrs Lewintan	9. Colapinto	13. Franchini	17. Joan L.	21. Doran	25. Klausen	29. ??
2. Alves	6. Alho	10. Stockwell	14. Fiorini	18. Dorst	22. Prodanov	26. Roosen	30. Okamoto
3. WARjr	7. Dechant	11. Tingelstad	15. Mrs Fiorini	19. Bell	23. Huang	27. Taniçli	31. Hitzer
4. Lewintan	8. Zatloukal	12. Todd	16. Lasenby	20. McClellan	24. Li	28. Burns	32. Moya



Waldyr Alves Rodrigues Jr

Publicado por Universia en Investigadores

En el ámbito de la Física Matemática, el tratamiento de los fundamentos lógicos y matemáticos...

Más información 

<http://www.arbolmat.com/>

N

- Plenary lecture: *Concept of the Lie derivative of spinor fields. A geometric motivated approach* (with Samuel WAINER)
- Summer School 1st lecture: *(Some) differential geometry and general relativity.*
- Summer School 2nd lecture: *Physical applications.*

GEOMETRIC ALGEBRA

E. ARTIN

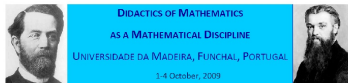
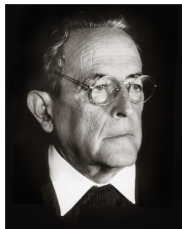
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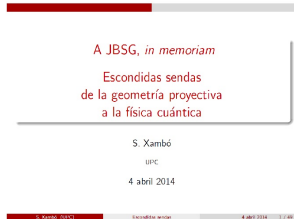
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A Clifford perspective on Klein's Geometry

SEBASTIAN XAMBÓ

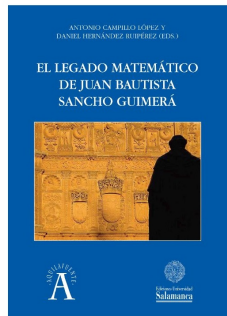
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 UNIVERSITAT POLITÈCNICA DE CATALUNYA
 08028 BARCELONA (SPAIN)



S. Xambó (UPC)

Escondidas sendas

4 abril 2014



WARJr Work

- The PhD thesis in nuclear physics (Università di Torino, 1971, advisor Cesare Rosseti) and the first 25 papers of WARJr (1972-1986) are, in general terms, about particle physics and relativity theory (mainly SR).
- 1980: Moved from the Physics to the Mathematics Institute.
- Alcebiades RIGAS asked him to deliver a series of lectures on relativity theory for MSc and PhD students. Suggested reference: R. K. SACHS & H. WU, *General Relativity for Mathematicians* (1977).
- Less than a full success: Mathematicians complained of “low mathematical rigor” and physicists “did not understand basic deductions and calculations in the language of **intrinsic differential geometry**”.

- 1927 W. PAULI: Zur Quantenmechanik des magnetischen electrons.
- 1928 P. A. M. DIRAC: The quantum theory of the electron.
- 1935 R. BRAUER, H. WEYL: Spinors in n dimensions.
- 1938 E. CARTAN: *Leçons sur la théorie des spineurs*.
- 1948 H. C. LEE: On Clifford algebras and their representations.
- 1950 Y. KAWADA, N. IWAHORI: On the structure and representations of Clifford algebras.
- 1954 C. CHEVALLEY: *The algebraic theory of spinors* (CW2).
- 1958 M. RIESZ: *Clifford numbers and spinors*.
- 1859 R. LIPSCHITZ (signed): Correspondence. *AM* **69**.
- 1964 M. ATIYAH, R. BOTT, A. SHAPIRO: Clifford modules.
- 1966 D. HESTENES: *Spacetime algebra*.

1967 D. HESTENES: Real spinor fields.

1969 I. R. PORTEOUS: *Topological geometry* (especially Ch 13).

1975 D. HESTENES: Observables, operators, and complex numbers in the Dirac theory.

1976 G. CASANOVA: *L'algèbre vectorielle*.

1982: F. BRACKX, R. DELANGHE, F. SOMMEN: *Clifford analysis*.

1984 D. HESTENES & G. SOBCZYK: *Clifford algebra to geometric calculus*.

1984 R. PENROSE, W. RINDLER: *Spinors and space-time*.

1987 I. BENN & R. TUCKER: *An introduction to spinors and geometry with applications in physics*.

1989 P. BUDINICH & A. TRAUTMAN: *The spinorial chessboard*.

- Launch of the **mathematical physics group** of IMECC-UNICAMP (Instituto de Matemática, Estatística e Computação Científica Unicamp).
- Discussions with colleagues lead to the study of **Clifford algebras and spinors**. Plans for applying these methods to mathematical physics problems.
- Advises several theses, including three defended in 1987:
 - VERA L. X. FIGUEIREDO: *Estrutura Spinorial Em Variedades Lorentzianas*.
 - ADOLFO MAIA JR.: *Potenciais Generalizados e Cargas Duais: Um Ensaio Sobre Monopolos Magnéticos*.
 - MARCIO A. DE FARIA ROSA: *Aplicações de Fibrados Principais e Teorias de Espaço-Tempo e Algumas Teorias Físicas*.

“My main motivation for applying CLIFFORD algebras methods in physics came from a very simple observation: The main physical theories of the last century,

- MAXWELL *electrodynamics*,
- DIRAC's *theory of electron*, and
- EINSTEIN's *general relativity*

describe three different kinds of fields (electromagnetic, spinor and gravitational). In the usual presentation in textbooks, however, these fields are described by mathematical objects of different nature.

So, I asked myself [**Waldyr's dream**]: *If one wants to make a unified theory, the first thing one should try is to represent these fields as objects of the same mathematical nature.*” (1.1.2017)

A SATISFACTORY FORMALISM FOR MAGNETIC MONOPOLES BY CLIFFORD ALGEBRAS [☆]

Marcio A. DEFARIA-ROSA ^a, Erasmo RECAMI ^{a,b,c} and Waldyr A. RODRIGUES Jr. ^a

^a *Department of Applied Mathematics, State University at Campinas, 13100 Campinas SP, Brazil*

^b *Dipartimento di Fisica, Università Statale di Catania, I-95129 Catania, Italy*

^c *INFN, Sezione di Catania, I-95129 Catania, Italy*

Received 3 March 1986

The problem of electromagnetism with magnetic monopoles is approached by the physically interesting and mathematically powerful formalism of Clifford algebras, which provides a natural language for Minkowski space-time (*Dirac algebra*) and euclidean space (*Pauli algebra*). A lagrangian and hamiltonian formalism is constructed for interacting monopoles, which overcomes many of the long-standing difficulties that are known to plague the approaches developed till now.

As a consequence, we can decompose F in Pauli algebra *either* as $F = E + H$ (in which case H is a Pauli pseudo-vector), *or* as [2]

$$F = E + iH,$$

in which case E and H are Pauli vectors.


[1] D. Hestenes, *Space-time algebra* (Gordon & Breach, New York, 1966);

[2] See e.g. E. Majorana, scientific manuscripts (ca. 1931), as reported in R. Mignani, E. Recami and M. Baldo, *Lett. Nuovo Cimento* 11 (1972) 568;

- 1992 Quintino Augusto GOMES DE SOUZA: *Dirac Operators on Riemann-Cartan-Weyl Spacetimes and the Nature of the Gravitational Field* N
- 1992 José Ricardo REZENDE ZENI: *Lorentz Transformations, Clifford Algebras and the Motion of Charged Particles.*
- 1993 Jayme VAZ JR.: *A Álgebra do Espaço-Tempo, O Spinor de Dirac-Hestenes e A Teoria do Eletron.*
- 1999 José Emilio MAIORINO: *Superluminal Solutions of the Relativistic Wave Equations and the Principle of Relativity.*
- 1999 Antonio Manuel MOYA: *Formalisimo Lagrangiano para Campos Multivetorias.*
- 2000 Virginia Velma FERNANDEZ: *Distortion and Rotation Extensors in the Gravitational Theories.*
- 2000 Alexandre Luis TROVON DE CARVALHO: *O Papel Algébrico dos Operadores Diferenciais no Formalismo Variacional.* N

- 1993: ICCA3 (Ghent)
- 1995: ICCA4 (Aachen)
- 1999: ICCA5 (Ixtapa-Zihuatanejo, México).
- 2001: ICCA6 (Cookville, Tennessee).
- 2005: ICCA7 (Toulouse)
- 2008: ICCA8 (Campinas)
- 2010: ICCA9 (Weimar)
- 2014: ICCA10 (Tartu)
- 2015: AGACSE 2015

8th International Conference of
**Clifford Algebras
 and their Applications
 Mathematical Physics**
 Campinas 2008 May 26-30



"For geometry, you know, is the gate of
 science, and the gate is so low and small
 that one can only enter it as a little child."

W. K. Clifford, Applications of Grassmann's Exterior Algebra, Dover, 1, 2nd Ed., 1968 (1970)

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




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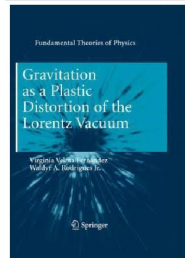
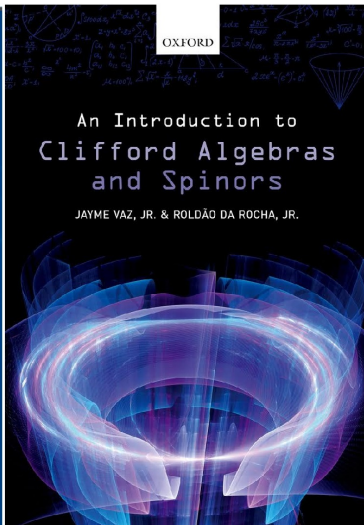
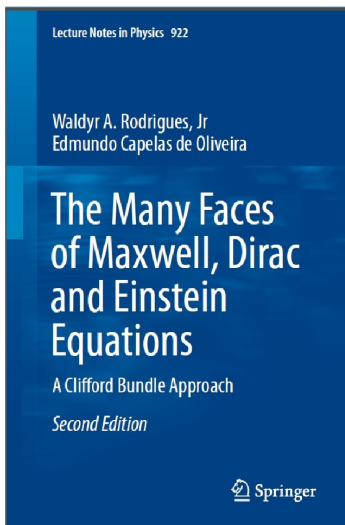
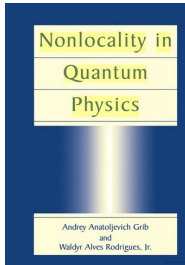
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- 1990 (with E. C. DE OLIVEIRA): Dirac and Maxwell equations in the Clifford and spin-Clifford bundles. *International Journal of Theoretical Physics* **29**. MR1057506 (91d:53021)
- 1995 (with Q. A. G. DE SOUZA and Y. BOZHKOV): The mathematical structure of Newtonian spacetime: Classical dynamics and gravitation. *Foundations of Physics* **25**. MR1342391 (96f:53101)
- 1996 (with J. VAZ JR. and M. PAVŠIČ): The Clifford bundle and the dynamics of the superparticle. *Banach Center Publications* **37**. MR1442741 (98i:81091)
- 1997 (with J.-Y. LU): On the existence of undistorted progressive waves (UPWs) of arbitrary speeds $0 \leq v < \infty$ in nature. *Foundations of Physics*, **27**. MR1452199 (98f:35144)
- 1999 (with A. A. GRIB): *Nonlocality in Quantum Physics*. 225 p.

- 2004: *Algebraic and Dirac–Hestenes spinors and spinor fields*. *Journal of Mathematical Physics* **45**. MR2067593 (2006b:81113)
- 2004 (with R. A. MOSNA): *The bundles of algebraic and Dirac–Hestenes spinor fields*. *Journal of Mathematical Physics* **45**. MR2067594 (2006b:81114)
- 2010 (with V. V. FERNÁNDEZ): *Gravitation as a plastic distortion of the Lorentz vacuum*. *Fundamental Theories of Physics* **168**. x + 153p. MR3012268
- 2012: *The nature of gravitational field and its legitimate energy-momentum tensor*. *Reports on Mathematical Physics* **69**.
- 2014 (with S. A. WAINER): *A Clifford Bundle Approach to the Differential Geometry of Branes*. *AACA* **24**.
- 2016 (with E. C. DE OLIVEIRA): *The Many Faces of Maxwell, Dirac and Einstein Equations* (2nd ed). *LNiP* **992**. XVI+587 p.



“I am proud to have formed a solid mathematical physics group at IMECC-UNICAMP and proud, e.g., that J. VAZ and R. DA ROCHA just published *An Introduction to Clifford Algebras and Spinors*” (2.1.2017)

- 1. Preliminaries [Tensor algebra].
- 2. Exterior algebra and Grassmann algebra.
- 3. Clifford, or geometric, algebra.
- 4. Classification and representation of the Clifford algebras.
- 5. Clifford algebras and associated groups [Lipschitz, Pin, Spin]
- 6. Spinors [Algebraic, classical and spinor operators].
- A. The standard two-component spinor formalism.

References to work of WARjr: [Figueiredo-Oliveira-W-1990-2 \[44\]](#), [Vaz-W-1993-2 \[54\]](#), [W-Rocha-Vaz-2005 \[124\]](#).

1. **Introduction.**
2. **Multivector and extensor calculus.** Fz-Moya-W-2001-2 [106]
3. **The hidden geometrical nature of spinors.** Chevalley-54, Benn-Tucker-87, Rocha-W-2006-1 [127].
4. **Some differential geometry.** DeRham-60, Sachs-Wu-77, Hestenes-Sobczyk-1984, Lawson-Michelsohn-89, Maia-Recami-W-Rosa-1990-1 [37], W-Oliveira-1990 [42], Fz-W-2010 [160], Leao-W-Wainer-2017 [184]
5. **Clifford bundle approach to the differential geometry of branes.** NotteCuello-W-Souza-2007 [147]
6. **Some issues on relativistic spacetime theories.** Weinberg-72, Matolcsi-W-1997-1 [89], W-Sharif-2001-2 [116], Giglio-W-2012-1 [166]
7. **Clifford and Dirac-Hestenes spinor fields.** Bleecker-81, Penrose-Rindler-1986, Naber-00, W-2004 [120], Oliveira-W-2004 [122] N

8. **Clifford algebra Lagrangian formalism in Minkowski spacetime.** Moya-Fz-W-2001-1 [104]
9. **Conservation laws on Riemann-Cartan and Lorentzian spacetimes.** Misner-Thorne-Wheeler-1973, Lasenby-Doran-Gull-1998, W-Souza-1993 [60], Bozhkov-W-1995 [72], Fz-Moya-W-2000 [103], NotteCuello-W-2009 [155], W-2012 [168], W-Wainer-2016-1 [178]. [149, 150]
10. **The DHE on a RCST and the meaning of active local Lorentz invariance.** W-Souza-Vaz-Lounesto-1996 [77]
11. **On the nature of the gravitational field.** Fz-W-2010 [160], W-2010 [161], NotteCuello-Rocha-W-2010 [162], W-2012 [168]
12. **On the many faces of Einstein equations.** Göckler-Schücker-87, Frankel-97, W-Oliveira-2004 [123]

13. **Maxwell, Dirac and Seiberg-Witten equations.**
Campolattaro-80, W-2003 [118].
14. **Superparticles and superfields.** Daviau-93, Varadarajan-00,
W-Souza-Vaz-1995 [74], W-Vaz-1998-2 [95], Grib-W-1999 [102]
15. **Maxwell, Dirac and Navier-Stokes equations.**
FabioRodrigues-W-Rocha-2012 [171]
16. **Magnetic like particles and Elko spinor fields.** W-2003
[118], Rocha-W-2006-1 [127], Oliveira-W-Vaz-2014-2 [174]
- A. **Principal bundles, vector bundles and connections.**
Kobayashi-Nomizu-63.

(From message 1/1/2017)

To sum up, what at first sight looked as fields of very different mathematical nature turned to be represented by objects of the same mathematical nature and their equations of motion can all be expressible in a form that looks the equation of motion of the others.

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- Maxwell and Dirac equations mathematically equivalent.
- Sub and superluminal phenomena.
- Einstein equation can be written as a Maxwell like equation.
- Poetical summary: I am not stating that these fields have the same physical ontology (in fact they do not), but it seems that GOD uses the same kind of mathematics in projecting these objects...

- 1992 and 1998: Zeferino Vaz Prize for Academic Merit (University of Campinas)
- 1995: Elected member of the Łódź Society of Sciences (Poland)
- 2010: Paul Sabatier Honor Medal (Paul Sabatier University)
- 2010: Elected member of the Russian Academy of Natural Sciences.
- 2012,...,2016: Editor in Chief of AACA (0.905 impact factor at end of his appointment)







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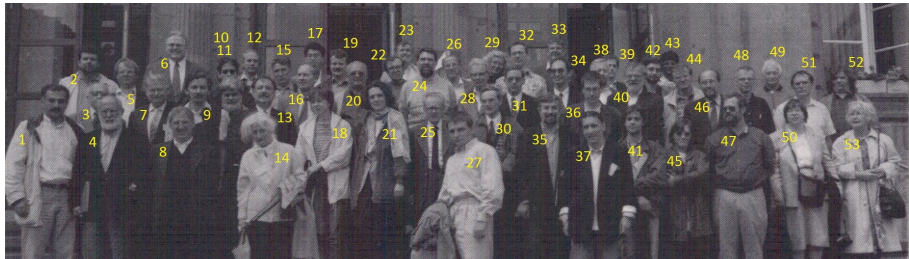
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Yuri Bozhkov, WARJr, Pamela Ramos, Stylianos Dimas (24.2.2017)



Waldyr was member of the Scientific Council of the “Centro de Lógica, Epistemologia e História da Ciência da UNICAMP”.





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arXiv.org > math-ph > arXiv:math-ph/0605008

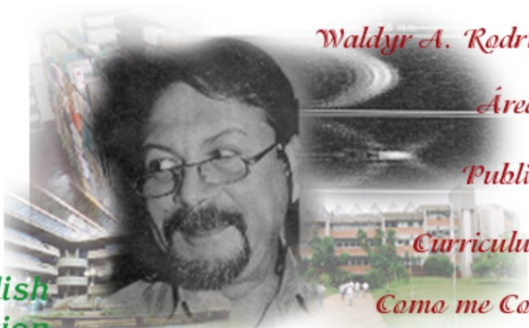
Mathematical Physics

Conservation Laws on Riemann-Cartan, Lorentzian and Teleparallel Spacetimes

Waldyr A. Rodrigues Jr, Quintino A. G. de Souza, Roldao da Rocha

(Submitted on 3 May 2006 (v1), last revised 12 Jan 2008 (this version, v13))

Waldyr Alves Rodrigues Jr.



Waldyr A. Rodrigues Jr.

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*English
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Wer immer strebend sich bemüht,
den können wir erlösen (Goethe, *Faust*)



N

**7th Conference on Applied Geometric Algebras
in Computer Science and Engineering**

**University of Campinas (UNICAMP)
Campinas (São Paulo), Brazil**

July 23-27, 2018

See you there!!

I want to begin by thanking Hennie de Schepper and the different committees, and especially to the scientific and organizing committees, for the invitation.

The idea of proposing to speak about the life and work of WARjr took form early in the June visit of Carlile LAVOR, of the University of Campinas, to Barcelona. The visit had been planned almost one year ago with two main goals: helping him in the organization of AGACSE 2018 in Campinas (July 23-27) and to do some work in the applications of GA to various questions.

The main trail that has lead us to this point started, at least formally, with AGACSE 2015 (Barcelona, July 27-31; about seventy participants). P

[On return to slide, go to next one (AGACSE 2015) and, after a brief pause, go to the next].

This picture was taken in the evening of July 30, 2015. This subgroup gathered to go to the social dinner downtown. On the way it met Gaudi's dragon at the back of the Pedralbes Palace.

Several people in the picture are also present here at ICCA11, and I hope it brings good memories to them of those days in Barcelona.

The third on the left is WARjr. If not physically here, his presence will be in the mind and hearts of all in this conference, and in many others outside, particularly those that could not come to this ICCA, and I believe that this will continue for many years to come on account of his rich scientific legacy: works, research school (students and colleagues), and his remarkable quixotic stance against all sorts of windmills.

AGACSE 2015 was the first occasion, and sadly the last, for me to meet Waldyr in person. At the end of that week, many things had happened that were driven by him. Here are those that seem to me more relevant:

- He delivered three one-hour lectures, two in the Summer School and a plenary in the conference. I'll come back to this a little later.
- The Proceedings would be published in a special volume of AACA and the editors would be Josep Manel Parra, Ramon Gonzalez Calvet, and myself as EiC of the project. These proceedings were published early this year and you can see details of how the process evolved in the Preface written by Parra and myself. There we acknowledge in particular the decisive support of Waldyr at the beginning, and that of Rafal Ablamowicz afterwards.
- AGACSE 2018 would be organized in Campinas. Carlile LAVOR, the leftmost in the picture, is the Chairman of the Organizing Committee.
- The Spanish Mathematical Society decided to include his profile in the portal that we colloquially call **ArbolMat**/MathTree (<http://www.arbolmat.com/>).

In the slide you can see the titles of his three lectures. For now remark that the words emphasized in blue point to themes that have been among his constant research passions.

The picture was taken during his plenary lecture and it is the one featured in his ArbolMat profile.

[Let me insert a brief aside to say that since the beginning of ArbolMat in 2011, we have published 68 profiles. An ArbolMat profile consists of a mention page (detail in the upper part of the slide) and a dossier on the academic evolution (accessed through “Otras informaciones”). I have taken the materials in Waldyr’s profile as a core input for my talk. They were prepared in close collaboration with him in the last months of 2016 and early January of this year.

P

Please allow me to tell you briefly where was I before AGACSE 2015. We studied Emil Artin's *Geometric Algebra* in 1966-1967 at the FM of the UB, following lectures by Professor Juan Bautista SANCHO GUIMERÁ. He was as passionate about mathematics and physics as Waldyr, he also supervised many students (ten years in Barcelona, until 1972, and in Salamanca, where he moved in that year, until his death in 2012), and both could concentrate for hours on their current topic, but otherwise they were completely opposite in one respect: whereas Waldyr was always extremely diligent to publish, Sancho's ideas were only, for the most part, communicated orally to his students.

Front page of my slides *A Clifford view of Klein's Geometry* presented in a conference held in Funchal (Madeira) in 2009 and of my lecture in April 2014 in the Symposium in memoriam of Sancho. The title of the talk, and of the paper published in the Proceedings volume, was (in English) *Hidden pathways from projective geometry to quantum physics* with the third part devoted to geometric algebra.

The “hidden pathways” phrase points to the poem “Vida retirada/Secluded life” of FRAY LUIS DE LEÓN, a XVI century Augustinian friar, theologian and academic admired by SANCHO. After imprisonment for four years in Valladolid by the Inquisition, Fray Luis began his first class in Salamanca on 29 January 1577 with the words *Dicebamus hesterna die...* (“As we were saying yesterday...”).

For the part on GA, I approached Manuel Parra and Ramon Gonzalez to seek their advice. This was just in the Spring before the Tartu ICCA and they managed –it was not that hard– to convince me to join them in organization of AGACSE 2015. I put all I could, institutionally and personally, for meeting that responsibility as best as possible. Among the many unexpected rewards of that decision I count having met Waldyr. So let us consider his work from a general perspective. P

The prestige of 'intrinsic differential geometry' at that time in relation to physics was based not only on its role in general relativity, but also because of the purely geometric formulation of gauge theories by means of fiber bundles (principal bundles with fiber a Lie group and the vector bundles associated to linear representations of that group). It seems clear that a key point for Waldyr's evolution was the fact that, in words of Andrej Trautman, "the definition of spinors on manifolds –unlike that of tensors– requires the use of fiber bundles".

Since the natural language for spinors is GA, the appeal at that point for trying to fuse the two languages must have had for Waldyr an irresistible appeal.

Let us consider the context in which this conception occurred by pointing out a few developments that concurred in it and which, for the most part, influenced the course of Waldyr thinking.

This was his fifth paper to be reviewed in MR, but the first with an authored review (Dominique Lambert):

1986 (with M. A. F. ROSA and E. RECAMI): A satisfactory formalism for magnetic monopoles by Clifford algebras. *Physics Letters B* **173**/3 (1986), 233-236. MR 87j:81267 (and MR 88c:81126, for Erratum 1987).

“The problem of electromagnetism with magnetic monopoles is approached by the physically interesting and mathematically powerful formalism of Clifford algebras, which provides a natural language for Minkowski space-time (Dirac algebra) and Euclidean space (Pauli algebra). A Lagrangian and Hamiltonian formalism is constructed for interacting monopoles, which overcomes many of the long-standing difficulties that are known to plague the approaches developed till now”.

The most relevant references are

[1] Hestenes, *STA* (1966) and

[2] E. Majorana, *Scientific manuscripts* (ca. 1931).

The latter is quoted as follows: "... we can decompose F [the electromagnetic field] in Pauli algebra *either* as $F = E + H$ (in which case H is a Pauli pseudo-vector), *or* [2] as $F = \mathbf{E} + \mathbf{iH}$, in which case \mathbf{E} and \mathbf{H} are Pauli vectors".

Note that Recami is the author of *Il caso Majorana* (Di Renzo Editore, Roma, 2001) and coeditor of *Ettore Majorana: Unpublished Research Notes on Theoretical Physics* (2009, 496 p), among other contributions *in memoriam* of Majorana. P

For a general reference on Cartan's geometries and variations thereof, one commendable book is:

R. W. Sharpe, *Differential Geometry: Cartan's generalization of Klein's Erlangen Program*. GTM, Springer, 1997.

As Waldyr retired in 1998, he took no more students after the year 2000.

P

0 Waldyr. 2 Hennie de Schepper. 19 Fred Brackx. 20 Wolfgang Sprössig. 21 Rafal Ablamowicz. 22 Matei Pavsic. 23 Anthony Lasenby. 28 Eduardo Bayro. 47 David Hestenes. 49 Eckhard Hitzer. 55 Jayme Vaz.

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[44] 1990 (with V. L. FIGUEIREDO and E. C. DE OLIVEIRA): Clifford algebras and the hidden geometrical nature of spinors. *Algebras, Groups, and Geometries* **7/2** (1990), 153-198. MR 92f:15015

[54] 1993 (with J. VAZ JR.): Equivalence of Dirac and Maxwell equations and quantum mechanics. *International Journal of Theoretical Physics* **32/6** (1993), 945-955. MR 94h:81051

[124] 2005 (with R. DA ROCHA and J. VAZ JR.): Hidden consequence of active local Lorentz invariance. *International Journal of Geometric Methods in Modern Physics* **2/2** (2005), 305-357.

This text does not replace P. Lounesto's *Clifford algebra and spinors* (2001, 2nd ed), and the common ground is approached quite differently.

(2) [106] Extensors. AACA

(3) Chevalley-54 and Benn-Tucker-87 already met before. [127] Where are ELKO spinor fields in Lounesto spinor field classification? MPL A.

(4) [37] Magnetic monopoles without string in the Kähler-Clifford algebra bundle: a geometrical interpretation. JMP. [42] Dirac and Maxwell equations in the Clifford and spin-Clifford bundles. JTP. [160] *Gravitation as a plastic distortion of the Lorentz vacuum*. [184] Concept of Lie derivative of spinor fields, a geometric motivated approach. AACA.

(5) [147] The square of the Dirac and spin-Dirac operators on a Riemann-Cartan space(time). RMP.

(6) [89] Spacetime model with superluminal phenomena. AGG. [116] Rotating frames in SRT: the Sagnac effect and related issues. FP. [166] Local inertial reference frames in Lorentzian and Riemann-Cartan spacetimes. AP.

- (7) [120] Algebraic and Dirac-Hestenes spinors and spinor fields. JMP. [122] Dotted and undotted algebraic spinor fields in general relativities. IJMP D.
- (8) [104] Lagrangian formalism for multiform fields on Minkowski spacetime. IJTP.
- (9) [60] The Clifford bundle and the nature of the gravitational field. FP. [72] Mass and energy in general relativity. GRG [103] Covariant derivatives on Minkowski manifolds. Ixtapa-Zihuatanejo (1999). [155] Freud's identity of differential geometry, the Einstein-Hilbert equations and the vexatious problem of the energy-momentum conservation in GR. AACAA. [168] nature of the gravitational field and its legitimate energy-momentum tensor. RMP. [178] Notes on the conservation laws, equations of motion of matter, and particle fields in Lorentzian and teleparallel de Sitter space-time structures. AMP.

- (10) [77] Dirac-Hestenes spinor fields on Riemann-Cartan spacetime. IJTP.
- (11) [160] *Gravitation as a plastic distortion of the Lorentz vacuum*. [161] Killing vector fields, Maxwell equations and Lorentzian spacetimes. AACA. [162] Some thoughts on geometries and on the nature of the gravitational field. JPM. [168] Nature of the gravitational field and its legitimate energy-momentum tensor. RMP.
- (12) [123] Clifford valued differential forms and some issues in gravitation, electromagnetism and “unified” theories. IJMP D.
- (13) [118] The relation between Maxwell, Dirac, and the Seiberg-Witten equations. IJMMS.
- (14) [74] Spinor fields and superfields as equivalence classes of exterior algebra fields. In Mathematics and its applications 321. [95] From electromagnetism to relativistic quantum mechanics. FP. [102] *Nonlocality in quantum physics*.

(15) [171] The Maxwell and Navier-Stokes that follow from Einstein equation in a spacetime containing a Killing vector Field. AIP CP.

(16) [118] The relation between Maxwell, Dirac, and the Seiberg-Witten equations. IJMMS. [127] Where are ELKO spinor fields in Lounesto spinor field classification? MPL A. [174] Elko spinor fields and massive magnetic like monopoles. IJTP.

P

Years of hard work (with my students and some collaborators) realized that dream and in so doing we proved that the Maxwell and Dirac equations are mathematically equivalent (in a well defined sense) for all solutions of Maxwell equations for which one of the Poincaré invariants is not null.

Moreover, this result lead us to discover that all relativistic wave equations have three classes of (free boundary) solutions, namely, subluminal, luminal and superluminal. In particular the superluminal solutions (which are such that only finite aperture approximations can be realized in the physical world and for which the peak travels at superluminal velocity for a while until arriving at the front of the wave) possess longitudinal electric and/or magnetic components. This generated interest of Motorola which financed in 1999 a research project to develop an antenna to launch this kind of waves. This research has been the seed for the creation of a new research

institute in Campinas (von Braun Labs), started from my (pos-doc) student Dario Sassi THOBER in 2000.

But returning to the original program, I discovered that Einstein equation can be written as a Maxwell like equation (with a current term depending on the gravitational potential, that makes the equation a nonlinear one) and that such an equation (and thus Maxwell and Dirac equation) could be written as a Navier-Stokes like equation.

X-waves (message 2/1/2017). The experimental production of finite aperture approximations to superluminal waves (which can be launched in physical space by special antennas) have been demonstrate in several experiments done long ago (see some references in a new paper of mine that I am sending attached). Concerning the Motorola experiment, almost all the research was classified material(*). However, I am sending attached a note of the

Motorola news informing that the experiment realized at Motorola labs in May 2001.

As mentioned above, I am sending also to you a first draft of a paper that I wrote during last month (and which is in way to arXiv today). In one of the sections I describe the X-wave, how to generate finite aperture approximations and the reshaping phenomena. Hope you will enjoy it.

P

Waldyr, Edmundo Capelas de Oliveira and André Kock Torres Assis (Assisi, Italy, 1989). They were attending a conference in Perugia University. P

Maria Paula, Renata, Maria Larissa. On 15 July 2017, Maria Paula send me the following words (my translation):

“His love for my mother and for the children was clear, but the greatest love in his life was, without doubt, his granddaughter Olívia Sanchez, the daughter of Maria Larissa born on 12/7/2014.

His great passions were bying, reading and studying books. At 32, there has been no day in my life in which I did no see him with a book in his hands. Even when he was sick or in hospital, he always asked me to bring him a book and his glasses.

What was funny about him is that when I had doubts about something (especially in college), I would ask him a problem and he would give me at least 5 references on the subject of doubt... That is, I thought I was going to have my problem solved quickly with his help and I left even with more doubts...! On personal matters, however, he always gave his opinion quite succinctly and, again, made me think –never gave ready answers.”

I want to express my gratitude to all the persons that have provided me advice or materials during the preparation of this work, and in particular to Manuel Parra, Maria Paula Grangeiro, Edmundo Capelas de Oliveira, Yuri Bozhkov, Fabio Rodrigues (son of Waldyr), Samuel Wainer, and Hilde de Ridder (for providing me copies of two papers that I could not find in Barcelona).

P

- [1] 1972: Calculation of the K_{l4} form factors in the soft pion formalism. *Atti delle Accademia delle Scienze di Torino* **106** (1972), 173-180.
- [2] 1974 (with N. J. PARADA and A. R. LOPES): On the Theory of Disordered Alloys. *Brazilian Journal of Physics* **4** (1974), 263-281.
- [3] 1974 (with A. Turtelli Jr. and M. LYKSYS): Commentary about the large transverse secondary momenta observed at the ISR-CERN. *Anais da Academia Brasileira de Ciências* **46** (1974), 197-201.
- [4] 1974 (with A. Turtelli Jr.): Pion Inclusive Distributions at Cosmic Ray Energies and Comparison with ISR Data. *Nuovo Cimento A* **23** (1974), 227-236.

- [5] 1976 (with V. Buonomano): A comment on a proposed crucial experiment to test Einstein's special theory of relativity. *Nuovo Cimento B* **34** (1976), 240-244.
- [6] 1977 (with C. A. P. Ceneviva): Discrete "fireball" masses in high energy collisions. *Acta Physica Polonica B* **8** (1977), 457-467.
- [7] 1979: Single particle Green's functions calculations of the electrical conductivity of strong correlated systems. *Brazilian Journal of Physics* **9** (1979), 109-122.
- [8] 1979 (with E. J. YOFFA and D. ADLER): Electronic correlations in narrow-band solids. *Physics Review B* **19** (1979), 1203-1212.

- [9] 1979 (with C. M. G. Lattes, Y. Fojumoto, et. al.): A new type of nuclear interaction in the $\Sigma E_\gamma > 2 \cdot 10^{14}$ eV. Brazil-Japan emulsion chamber collaboration, *AIP Conference Proceedings* **49**, *Particles and Fields* **16** (1979), 317-333.
- [10] 1979 (with C. M. G. Lattes, Y. Fojumoto, et. al.): Multiple meson production in the $\Sigma E_\gamma \geq 2 \cdot 10^{13}$ eV region. Brazil-Japan emulsion chamber collaboration, *AIP Conference Proceedings* **49**, *Particles and Fields* **16** (1979), 94-109.
- [11] 1979 (with C. M. G. Lattes, Y. Fojumoto, et. al.): Baryon pair production with large decay Q-value. Brazil-Japan emulsion chamber collaboration, *AIP Conference Proceedings* **49**, *Particles and Fields* **16** (1979), 145-151.
- [12] 1980 (with J. Dias de Deus): Centauro, Geminion and multi-pion events. *Nuovo Cimento A* **55** (1980), 34-44.

- [13] 1982 (with E. RECAMI): Antiparticles from special relativity with orthochronous and antichronous Lorentz transformations. *Foundations of Physics* **12**/7 (1982), 709-718. MR 831:83006 (and MR 87b:83007 for Erratum 1983).
- [14] 1982 (with C. A. P. Ceneviva): Objetividade, Convencionalismo e a Teoria da Relatividade. *Cadernos de História e Filosofia da Ciência* **3** (1982), 59-83.
- [15] 1983: The standard of length in the theory of relativity and Ehrenfest paradox. *Nuovo Cimento B* **74** (1983), 199-211.
- [16] 1983 (with P. Ammiraju and E. RECAMI): Chirons, Centauros, Geminions, pion production: A phenomenological and theoretical analysis. *Nuovo Cimento A* **78** (1983), 172-204.

- [17] 1983 (with E. RECAMI and P. Smrz): Some applications of non-Hermitian operators in quantum mechanics and quantum field theory. *Hadronic Journal* **6** (1983), 1773-1789.
- [18] 1984: Is Lorentz invariance an exact symmetry of nature? *Hadronic Journal* **7/3** (1984), 436-455. MR 87i:83007
- [19] 1984 (with J. Tiomno): Einstein's special relativity versus Lorentz's aether theory. Volume dedicated to Mário Schönberg, *Brazilian Journal of Physics* **14** (1984), 450-465.
- [20] 1985: Lorentz-invariant clocks do not exist. *Lettere al Nuovo Cimento* (2) **44/7** (1985), 510-512. MR 87d:83008
- [21] 1985 (with J. Tiomno): On experiments to detect failures of relativity theory. *Foundations of Physics* **15** (1985), 945-961.

- [22] 1985 (with M. A. F. ROSA): Theory of the Michelson–Morley experiment in a gravitational field. *Lettere Nuovo Cimento* **44** (1985), 437-441.
- [23] 1985 (with E. RECAMI): Tachyons: May they have a role in elementary particle physics? *Progress in Particles and Nuclear Physics*
- [24] 1986 (with E. RECAMI): A model-theory for tachyons in two dimensions. *Proceedings of the Sir Arthur Eddington centenary symposium, Vol. 3* (Nagpur, 1984), 151-203. World Scientific Publishing, Singapore, 1986.
- [25] 1986 (with M. A. F. ROSA): A comment on the null geodesics equation in the Schwarzschild geometry. *Brazilian Journal of Physics* **16** (1986), 535-540.

- [26] 1986 (with M. A. F. ROSA and E. RECAMI): A satisfactory formalism for magnetic monopoles by Clifford algebras. *Physics Letters B* **173**/3 (1986), 233-236. MR 87j:81267 (and MR 88c:81126, for Erratum 1987).
- [27] 1986 (with Q. A. G. DE SOUZA): A comment on the proof of Noether's theorem in smooth manifolds. *Brazilian Journal of Physics* **16** (1986), 541-549.
- [28] 1986 (with E. RECAMI and M. FORCASTORO-DECKER): Os taquions. *Ciência Hoje* **5** (1986), 48-50.
- [29] 1988 (with E. RECAMI, A. MAIA Jr., and M. A. F. ROSA): Magnetic monopoles without string by Kähler-Clifford algebra: a satisfactory formalism. *SILARG, VI* (Rio de Janeiro, 1987), 320-332, World Scientific Publishing, Singapore, 1988.

- [30] 1989 (with A. MAIA JR.): Grassmann's Fields and Generalized Magnetic Monopoles. *Brazilian Journal of Physics* **19** (1989), 292-305.
- [31] 1989 (with E. RECAMI, A. MAIA Jr., and M. A. F. ROSA): The classical problem of the charge and pole motion. A satisfactory formalism by Clifford algebras. *Physics Letters B* **220**/1-2 (1989), 195-199. MR 90b:78005
- [32] 1989 (with M. A. F. ROSA): The meaning of time in the theory of relativity and "Einstein's later view of the twin paradox". *Foundations of Physics* **19**/6 (1989), 705-724. MR 90k:83006
- [33] 1989 (with M. A. F. ROSA): A geometrical theory of nontopological magnetic monopoles. *Modern Physics Letters A* **4**/2 (1989), 175-184. MR 91b:53091

- [34] 1989 (with M. A. F. ROSA): Physico-mathematical approach to generalized monopoles without string. *Hadronic Journal* **12**/4 (1989), 187-212. MR 91f:81240
- [35] 1989 (with E. C. DE OLIVEIRA): A comment on the twin paradox and the Hafele-Keating experiment. *Physics Letters A* **140**/9 (1989), 479-484. MR 90m:83007
- [36] 1989 (with V. L. FIGUEIREDO): A new approach to the spinor structure of space-time. *General relativity and gravitational physics* (Cavalese, 1988), 467-471, World Scientific Publishing, Teaneck, NJ, 1989.

- [37] 1990 (with A. MAIA Jr., E. RECAMI, and M. A. F. ROSA): Magnetic monopoles without string in the Kähler-Clifford algebra bundle: a geometrical interpretation. *Journal of Mathematical Physics* **31**/2 (1990), 502-505. MR 91d:81158 (and MR 92b:81225 for Erratum).
- [38] 1990 (with M. E. F. SCANAVINI and L. B. DE ALCANTARA): Formal structures, the concepts of covariance, invariance, equivalent reference frames, and the principle of relativity. *Foundations of Physics Letters* **3**/1 (1990), 59-79. MR 91b:83005
- [39] 1990: A comment: "On generalized electromagnetism and Dirac algebra" [Found. Phys. 19 (1989), no. 2, 125-159; MR0984198] by David Fryberger. *Foundations of Physics Letters* **3**71 (1990) 95-99. MR 91d:81106

- [40] 1990 (with A. MAIA Jr., E. RECAMI, and M. A. F. ROSA): Magnetic monopoles without string in the Kähler-Clifford algebra bundle: a geometrical interpretation of a satisfactory formalism. *Modern Physics Letters A* **5**/8 (1990), 543-549. MR 91i:81106 31
- [41] 1990 (with V. L. FIGUEIREDO and E. C. DE OLIVEIRA): Covariant, algebraic, and operator spinors. *International Journal of Theoretical Physics* **29**/4 (1990), 371-395. MR 91d:5302
- [42] 1990 (with E. C. DE OLIVEIRA): Dirac and Maxwell equations in the Clifford and spin-Clifford bundles. *International Journal of Theoretical Physics* **29**/4 (1990), 397-412. MR 91d:53021
- [43] 1990 (with V. L. FIGUEIREDO): Real spin-Clifford bundle and the spinor structure of space-time. *International Journal of Theoretical Physics* **29**/4 (1990), 413-424. MR 91d:53022.

- [44] 1990 (with V. L. FIGUEIREDO and E. C. DE OLIVEIRA): Clifford algebras and the hidden geometrical nature of spinors. *Algebras, Groups, and Geometries* **7/2** (1990), 153-198. MR 92f:15015
- [45] 1990 (with J. R. ZENI): Finite form of a generic proper orthochronous Lorentz transformation and its dynamical interpretation. *Brazilian Journal of Physics* **20** (1990), 377-384.
- [46] 1990 (with J. R. ZENI): The exponential of the generators of the Lorentz group and the solution of the Lorentz force equation. *Hadronic Journal* **13/4** (1990), 317-323. MR 92b:83007
- [47] 1991 (with Q. A. G. DE SOUZA): A Clifford bundle approach to gravitational theory. *Proceeding of the 7th Simposio Latino Americano de Relatividad y Gravitacion, SILARG VII*, 220-226, World Scientific Publishing, River Edge, NJ, 1991.

- [48] 1991 (with E. RECAMI): On magnetic monopoles (without string) and the Clifford bundle formalism. *Annales de la Fondation Louis de Broglie* **16** (1991), 1-12.
- [49] 1991 (with P. Ammiraju, E. RECAMI, J. ROVERSI, and V. T. ZANCHIN): Hadronic mass spectra in a unified approach of strong and gravitational theory. *Hadronic Journal* **14** (1991), 441-457.
- [50] 1992 (with J. R. ZENI): A thoughtful study of proper orthochronous Lorentz transformations by Clifford algebras. *An International Journal of Modern Physics A* **7/8** (1992), 1793-1817. MR 93d:15041

- [51] 1993 (with J. VAZ JR. and E. RECAMI): A generalization of Dirac nonlinear electrodynamics, and spinning charged particles. *Foundations of Physics* **23**/3 (1993), 469-485. MR 94c:83054. arXiv (12.3.1998)
- [52] 1993 (with J. VAZ JR. and E. RECAMI): Free Maxwell equations, Dirac equation and non-dispersive de Broglie wave-packets. *Courants, amers écueils en microphysique/Directions in microphysics*, 379-292. *Fondation Louis de Broglie*, Paris, 1993.
- [53] 1993 (with J. VAZ JR.): A spinor representation of Maxwell equations and the Dirac equation. *Hadronic Journal* **16** (1993), 129-135. MR 94a:81049

- [54] 1993 (with J. VAZ JR.): Equivalence of Dirac and Maxwell equations and quantum mechanics. *International Journal of Theoretical Physics* **32**/6 (1993), 945-955. MR 94h:81051
- [55] 1993 (with J. VAZ JR.): A basis for double solution theory. *Clifford algebras and their applications in mathematical physics*, (Deinze, 1993), 345-351, *Fundamental Theories of Physics* **55**, Kluwer Academic Publishers, Dordrecht, 1993.
- [56] 1993 (with J. VAZ JR.): Comments on Fryberger's approach to generalized electromagnetism. *Advances in Applied Clifford Algebras* **3**/2 (1993), 139-146. MR 94c:78004
- [57] 1993 (with R. L. MONACO): New integral representation of the solutions of the Schrödinger equation with arbitrary potentials. *Physics Letters A* **179**/4-5 (1993), 235-238. MR 94h:81026

- [58] 1993 (with J. E. MAIORINO and J. R. ZENI): The relationship between 2-spinors and rotations. *Algebras, Groups, and Geometries* **10**/1 (1993), 53-72. MR 94i:15023
- [59] 1993 (with M. PAVŠIČ, E. RECAMI, G. D. MACCARRONE, F. RACITI, and G. SALESI): Spin and electron structure. *Physics Letters B* **318**/3 (1993), 481-488. MR 94h:81163. arXiv (19.3.2002)
- [60] 1993 (with Q. A. G. DE SOUZA): The Clifford bundle and the nature of the gravitational field. *Foundations of Physics* **23**/11 (1993), 1465-1490. MR 95c:83054
- [61] 1993 (with J. VAZ JR., E. RECAMI and G. SALESI): About Zitterbewegung and electron structure. *Physics Letters B* **318**/4 (1993), 623-628. MR 95a:81298. arXiv (14.3.1998, corrected version)

- [62] 1993: Zitterbewegung and electron structure. *Clifford algebras and their applications in mathematical physics*, (Deinze, 1993), 397-404, *Fundamental Theories of Physics* **55**, Kluwer Academic Publishers, Dordrecht, 1993.
- [63] 1993 (with J. VAZ JR.): Zitterbewegung and the Electromagnetic Field of the Electron. *Physics Letters B* **319** (1993), 203-208.
- [64] 1993 (with J. E. MAIORINO & J. R. ZENI): Do neutron interferometric experiments implies that the neutron wave function is a covariant Pauli spinor. *Advances in Applied Clifford Algebras* **3** (1993), 21-28.

- [65] 1994 (with A. MAIA JR.): A generalized Dirac's quantization condition for phenomenological nonabelian magnetic monopoles. *Modern Physics Letters A* **9**/1 (1994), 81-88. MR 94m:81134
- [66] 1994 (with D. L. R. CAMPODÓNICO, Q. A. G. DE SOUZA, and J. VAZ JR.): The effective Riemann-Cartan-Weyl geometry generated by a Dirac-Hestenes spinor field. *Algebras, Groups, and Geometries* **11** (1994), 23-35. MR 95f:53129
- [67] 1994 (with Q. A. G. DE SOUZA): The Dirac operator and the structure of Riemann-Cartan-Weyl spaces. *Gravitation: the spacetime structure* (Águas de Lindóia, 1993), 179-212, World Scientific Publishing, River Edge, NJ, 1994.

- [68] 1994 (with J. VAZ JR.): About the equations of electromagnetism and quantum mechanics. *Gravitation: the spacetime structure* (Águas de Lindóia, 1993), 213-219, World Scientific Publishing, River Edge, NJ, 1994.
- [69] 1994 (with R. L. MONACO and G. G. CABRERA): A quantum spin-orbit gravitational coupling. *Gravitation: the spacetime structure* (Águas de Lindóia, 1993), 373-377, World Scientific Publishing, River Edge, NJ, 1994.
- [70] 1994 (with Q. A. G. DE SOUZA and J. VAZ JR.): Lagrangian formulation in the Clifford bundle of Dirac-Hestenes equation on a Riemann-Cartan spacetime. *Gravitation: the spacetime structure* (Águas de Lindóia, 1993), 534-543, World Scientific Publishing, River Edge, NJ, 1994.

- [71] 1995 (with Q. A. G. DE SOUZA and Y. BOZHKOV): The mathematical structure of Newtonian spacetime: Classical dynamics and gravitation. *Foundations of Physics* **25**/6 (1995), 871-924. MR 95f:53101
- [72] 1995 (with Y. BOZHKOV): Mass and energy in general relativity. *General Relativity Gravitation* **27**/8 (1995), 813-819.
- [73] 1995 (with R. L. MONACO and R. E. LAGOS): A Riemann integral approach to Feynman's path integral. *Foundations of Physics Letters* **8**/4 (1995), 365-373. MR 96f:58026
- [74] 1995 (with Q. A. G. DE SOUZA and J. VAZ JR.): Spinor fields and superfields as equivalence classes of exterior algebra fields. *Clifford algebras and spinor structures*, 177-198. *Mathematics and Its Applications* **321**, Kluwer Academic Publishers, Dordrecht, 1995.

- [75] 1995 (with M. PAVŠIČ and E. RECAMI): Electron structure, Zitterbewegung and a new non-linear Dirac-like equation. *Hadronic Journal* **18**, 97-118. arXiv (14.3.1998)
- [76] 1995 (with E. RECAMI, F. RACITI and V. T. ZANCHIN): Micro-universes and “strong black holes”: a purely geometric approach to elementary particles. arXiv (04.9.1995)
- [77] 1996 (with Q. A. G. DE SOUZA, J. VAZ JR. and P. LOUNESTO): Dirac-Hestenes spinor fields on Riemann-Cartan spacetime. *International Journal of Theoretical Physics* **35**/9 (1996), 1849-1900. arXiv (09.7.1996)
- [78] 1996 (with J. E. MAIORINO): A unified theory for construction of arbitrary speeds ($0 \leq v < \infty$) solutions of the relativistic wave equations. *Random Operators and Stochastic Equations* **4**/4 (1996), 355-400. arXiv (27.10.1997)

- [79] 1996 (with J. VAZ JR. and M. PAVŠIČ): The Clifford bundle and the dynamics of the superparticle. *Generalizations of complex analysis and their applications in physics* (Warsaw/Rynia, 1994), Banach Center Publications, **37/1** (1996), 295-314.
- [80] 1996 (with J. VAZ JR.): Spinors as differential forms, and applications to electromagnetism and quantum mechanics. *Gravity, particles and space-time*, 307-344. World Scientific Publishing, River Edge, NJ, 1996.
- [81] 1996 (with J. ŁAWRYNOWICZ and L. WOJTCZAK): Clifford-algebraical approach to particle lifetimes. *Bulletin de la Société des Sciences et des Lettres de Łódź. Série: Recherches sur les Déformations* **21** (1996), 57-63.

- [82] 1996 (with A. L. T. DE CARVALHO): A nest topology for Minkowski spacetime. *Boletim da Sociedade Paranaense de Matematica* (2) **16**/1-2 (1996), 23-38.
- [83] 1997 (with J.-Y. LU): On the existence of undistorted progressive waves (UPWs) of arbitrary speeds $0 \leq v < \infty$ in nature. *Foundations of Physics*, **27**/3 (1997), 435-508. arXiv (12.6.1996 v1, 16.10.1997 v4)
- [84] 1997 (with R. L. MONACO): The exact Bohr-Sommerfeld quantization rule. *Random Operators and Stochastic Equations* **5**/2 (1997), 197-202.
- [85] 1997 (with J. VAZ JR.): Maxwell and Dirac theories as an already unified theory. The theory of the electron (Cuautitlán Izcalli, 1995). *Advances in Applied Clifford Algebras* **7**/supplement (1997), 369-386. arXiv (25.11.1995)

- [86] 1997 (with J. VAZ JR.): On the equation $\nabla a = \kappa a$. *Boletim da Sociedade Paranaense de Matematica* (2) **17**/1-2 (1997), 19-24 (1998). arXiv (20.6.1996)
- [87] 1997 (with J. VAZ JR.): Subluminal and superluminal solutions in vacuum of the Maxwell equations and the massless Dirac equation. The theory of the electron (Cuautitlán Izcalli, 1995). *Advances in Applied Clifford Algebras* **7**/supplement (1997), 457-466. arXiv (25.11.1995)
- [88] 1997 (with S. DE LEO): Quantum mechanics: from complex to complexified quaternions. *International Journal of Theoretical Physics* **36**/12 (1997), 2725-2757.
- [89] 1997 (with T. MATOLCSI): Spacetime model with superluminal phenomena. *Algebras, Groups, and Geometries* **14** (1997), 1-16 arXiv (12.6.1996)

- [90] 1997 (with T. MATOLCSI): The geometry of space-time with superluminal phenomena. *Algebras, Groups, and Geometries* **14**/1 (1997), 1-16. arXiv (20.10.1997)
- [91] 1997 (with V. S. BARASHENKOV): Launching of non-dispersive superluminal beams. arXiv (20.10.1997)
- [92] 1997 (with J. E. MAIORINO): Faster than light? arXiv (21.10.1997 v1, 19.11.1997 v2)
- [93] 1998 (with E. C. DE OLIVEIRA): Superluminal Electromagnetic Waves in Free Space. *Annalen der Physik* **7** (1998), 654-662.

- [94] 1998 (with J. VAZ JR.): Subluminal and superluminal electromagnetic waves and the lepton mass spectrum. *Clifford algebras and their application in mathematical physics* (Aachen, 1996), 319-346. *Fundamental Theories of Physics* **94**, Kluwer Academic Publishers, Dordrecht, 1998. arXive (30.7.1996 v1, 31.7.1996 v2)
- [95] 1998 (with J. VAZ JR.): From electromagnetism to relativistic quantum mechanics. Invited papers dedicated to Asim O. Barut, Part III. *Foundations of Physics* **28**/5 (1998), 789-814.
- [96] 1998 (with S. DE LEO): Quaternionic electron theory: Dirac's equation. *International Journal of Theoretical Physics* **37**/5 (1998), 1511-1529. arXiv (06.6.1998)

- [97] 1998 (with S. DE LEO): International Journal of Theoretical Physics Quaternionic electron theory: geometry, algebra, and Dirac's spinors. *International Journal of Theoretical Physics* **37**/6 (1998), 1707-1720. arXiv (06.6.1998)
- [98] 1998 (with J. E. MAIORINO and Y. BOZHKOV): New solutions of the main relativistic wave equations. *Geometry Seminars*, 1996-1997 (Bologna), 201-229. Università di Bologna, Bologna, 1998.
- [99] 1998 (with S. DE LEO and J. VAZ JR.): Complex geometry and Dirac equation. *International Journal of Theoretical Physics* **37** (1998), 2415-2431. arXiv (17.5.1999)
- [100] 1999 (with A. K. T. ASSIS and A. J. MANIA): The electric field outside a stationary resistive wire carrying a constant current. *Foundations of Physics* **29**/5 (1999), 729-753.

- [101] 1999 (with S. DE LEO, Z. OZIEWICZ and J. VAZ JR.): The Dirac-Hestenes Lagrangian. *International Journal of Theoretical Physics* **38**/9 (1999), 2349-2369. arXiv (3.6.1999)
- [102] 1999 (with A. A. GRIB): *Nonlocality in quantum physics*. Kluwer Academic Publishers, 1999.
- [103] 2000 (with V. V. FERNÁNDEZ and A. M. MOYA): Covariant derivatives on Minkowski manifolds. *Clifford algebras and their applications in mathematical physics*, Volume 1 (Ixtapa-Zihuatanejo, 1999), 367-391. *Progress in Physics* **18**, Birkhäuser Boston, Boston, MA, 2000.

- [104] 2001 (with A. M. MOYA and V. V. FERNÁNDEZ):
Lagrangian formalism for multiform fields on Minkowski
spacetime. Clifford algebras and their applications (Ixtapa,
1999). *International Journal of Theoretical Physics* **40**/1
(2001), 299-314. arXiv (04.2.2003)
- [105] 2001 (with V. V. FERNÁNDEZ and A. M. MOYA):
Euclidean Clifford algebra. *Advances in Applied Clifford
Algebras* **11**/S3 (2001), 1-21. arXiv (13.12.2002 v1,
18.12.2002 v2)
- [106] 2001 (with V. V. FERNÁNDEZ and A. M. MOYA):
Extensors. *Advances in Applied Clifford Algebras* **11**/S3
(2001), 23-40. arXiv (16.12.2002)

- [107] 2001 (with A. M. MOYA and V. V. FERNÁNDEZ): Metric tensor vs. metric extensor. *Advances in Applied Clifford Algebras* **11**/S3 (2001), 41-48. arXiv (16.12.2002 v1, 18.12.2002 v2)
- [108] 2001 (with A. M. MOYA and V. V. FERNÁNDEZ): Metric Clifford algebra. *Advances in Applied Clifford Algebras* **11**/S3 (2001), 49-68. arXiW (16.12.2002)
- [109] 2001 (with A. M. MOYA and V. V. FERNÁNDEZ): Multivector functions of a real variable. *Advances in Applied Clifford Algebras* **11**/S3 (2001), 69-77. arXiv (17.12.2002)
- [110] 2001 (with A. M. MOYA and V. V. FERNÁNDEZ): Multivector functions of a multivector variable. *Advances in Applied Clifford Algebras* **11**/S3 (2001), 79-91. See /rf. (17.12.2002 v1, 18.12.2002 v2)

- [111] 2001 (with A. M. MOYA and V. V. FERNÁNDEZ): Multivector Functionals. *Advances in Applied Clifford Algebras* **11**/S3 (2001), 99-109. arXiv (17.12.2002 v1, 18.12.2002 v2)
- [112] 2001 (with A. L. T. DE CARVALHO): The non sequitur mathematics and physics of the “new electrodynamics” proposed by the AIAS group. *Random Operators and Stochastic Equations* **9**/2 (2001), 161-206. arXiv (06.2.2003 v1, 25.7.2006 v5)
- [113] 2001 (with E. C. DE OLIVEIRA, D. S. THOBER and A. L. XAVIER JR.): Causal explanation for observed superluminal behavior of microwave propagation in free space. *Physics Letters A* **284**/6 (2001), 217-224. arXiv (15.12.2000 v1, 11.5.2001 v4)

- [114] 2001 (with E. C. DE OLIVEIRA, D. S. THOBER and A. L. XAVIER JR.): Thoughtful comments on “Bessel beams and signal propagation” [Phys. Lett A 278 (2000), no. 1-2, 6-8; MR1811275] by D. Mugnai. *Physics Letters A* **284**/6 (2001), 296-303. arXiv (27.3.2001 v1, 29.5.2001 v4)
- [115] 2001 (with M. SHARIF): Equivalence principle and the principle of local Lorentz invariance. *Foundations of Physics* **31**/12 (2001), 1785-1806. Corrigenda: *Foundations of Physics* **32**/5 (2002), 811-812. arXiv (04.2.2003)
- [116] 2001 (with M. SHARIF): Rotating frames in SRT: the Sagnac effect and related issues. *Foundations of Physics* **31**/12 (2001), 1767-1783. arXiv (04.2.2003)

- [117] 2001 (with E. C. DE OLIVEIRA): Finite energy superluminal solutions of Maxwell equations. *Physics Letters A* **291**/6 (2001), 367-370. arXiv (29.5.2001 v1, 05.11.2001 v4)
- [118] 2003: The relation between Maxwell, Dirac, and the Seiberg-Witten equations. *International Journal of Mathematics and Mathematical Sciences* **2003**/43 (2003), 2707-2734. arXiv (10.12.2002 v1, 07.12.2012 v4)
- [119] 2003 (with J. ŁAWRYNOWICZ and L. WOJTCZAK): Stochastic electrodynamics in Clifford-analytical formulation related to entropy-depending structures. *Bulletin de la Société des Sciences et des Lettres de Łódź. Série: Recherches sur les Déformations* **41** (2003), 69-87.

- [120] 2004 Algebraic and Dirac–Hestenes spinors and spinor fields. *Journal of Mathematical Physics* **45**/7 (2004), 2908-2944. arXiv (10.12.2002 v1, 31.5.2005 v6)
- [121] 2004 (with R. A. MOSNA): The bundles of algebraic and Dirac–Hestenes spinor fields. *Journal of Mathematical Physics* **45**/7 (2004), 2945-2966. arXiv (10.12.2002 v1, 15.6.2004 v5)
- [122] 2004 (with E. C. DE OLIVEIRA): Dotted and undotted algebraic spinor fields in general relativities. *International Journal of Modern Physics D* **13**/8 (2004), 1637-1659. [Erratum: **14** (2005), 185] arXiv (13.7.2004 v1, 03.11.2004 v3). Expanded version (including [123]): arXiv (04.11.2003 v1, 08.12.2004 v5)

- [123] 2004 (with E. C. DE OLIVEIRA): Clifford valued differential forms, and some issues in gravitation, electromagnetism and “unified” theories. *International Journal of Modern Physics D* **13/9** (2004), 1879-1915. [Erratum: **14** (2005), 186] arXiv (13.7.2004 v1, 16.1.2008 v8) Expanded version (including [122]): arXiv (04.11.2003 v1, 08.12.2004 v5)
- [124] 2005 (with R. DA ROCHA and J. VAZ JR.): Hidden consequence of active local Lorentz invariance. *International Journal of Geometric Methods in Modern Physics* **2/2** (2005), 305-357. arXiv (26.1.2005 v1, 25.7.2006 v6)
- [125] 2005 (with Q. A. G. DE SOUZA): An ambiguous statement called the “tetrad postulate” and the correct field equations satisfied by the tetrad fields. *International Journal of Modern Physics D* **14/12** (2005), 2095-2150. arXiv (30.11.2004 v1, 06.1.2008 v12)

- [126] 2006: A comment on emergent gravity. arXiv (27.2.2006 v1, 27.3.2006 v2).
- [127] 2006 (with R. DA ROCHA): Where are ELKO spinor fields in Lounesto spinor field classification? *Modern Physics Letters A* **21**/1 (2006), 65-74. arXiv (29.6.2005 v1, 03.8.2005 v3)
- [128] 2006 (with R. DA ROCHA): The Einstein-Hilbert Lagrangian density in a two-dimensional spacetime is an exact differential. *Modern Physics Letters A* **21**/19 (2006), 1519-1527. arXiv (14.12.2005 v1, 04.7.2006 v7)
- [129] 2006 (with R. DA ROCHA): The Dirac-Hestenes equation for spherical symmetric potentials in the spherical and Cartesian gauges. *International Journal of Modern Physics A* **21**/19-20 (2006), 4071-4082. arXiv (09.1.2006 v1, 04.7.2006 v2)

- [130] 2006 (with A. M. MOYA & V. V. FERNÁNDEZ): Geometric algebras. arXiv (31.1.2005 v1, 30.8.2006 v4)
- [131] 2006 (with A. M. MOYA & V. V. FERNÁNDEZ): Metric and gauge extensors. arXiv (31.1.2005 v1, 30.8.2006 v2)
- [132] 2006 (with A. M. MOYA & V. V. FERNÁNDEZ): Extensors in geometric algebras. arXiv (31.1.2005 v1, 30.8.2006 v2)
- [133] 2006 (with A. M. MOYA & V. V. FERNÁNDEZ): Covariant derivatives of multivector and extensor fields. arXiv (31.1.2005 v1, 30.8.2006 v2)
- [134] 2006 (with V. V. FERNÁNDEZ & A. M. MOYA): Metric compatible covariant derivatives. arXiv (31.1.2005 v1, 30.8.2006 v2)

- [135] 2006 (with V. V. FERNÁNDEZ & A. M. MOYA): Derivative operators in metric and geometric structures. arXiv (31.1.2005 v1, 30.8.2006 v2)
- [136] 2007 (with E. C. DE OLIVEIRA): A comment on: “On some contradictory computations in multi-dimensional mathematics” [Nonlinear Analysis 63 (2005), no. 5-7, 725-734; MR2188145] by L. A. V. Carvalho. *Nonlinear Analysis* **67**/7 (2007), 2316-2320. arXiv (27.3.2006)
- [137] 2007 (with E. A. NOTTE-CUELLO): A Maxwell-like formulation of gravitational theory in Minkowski spacetime. *International Journal of Modern Physics D* **16**/6 (2007), 1027-1041. arXiv (07.8.2006 v1, 23.6.2009 v5)

- [138] 2007 (with V. V. FERNÁNDEZ, A. M. MOYA and E. A. NOTTE-CUELLO): Parallelism structure on a smooth manifold. *Algebras, Groups, and Geometries* **24/2** (2007), 129-153. arXiv (18.3.2007)
- [139] 2007 (with V. V. FERNÁNDEZ and A. M. MOYA): Geometric algebras and extensors. *International Journal of Geometric Methods in Modern Physics* **4/6** (2007), 927-964. arXiv (03.3.2007 v1, 29.11.2007 v2)
- [140] 2007 (with V. V. FERNÁNDEZ and A. M. MOYA): Geometric and extensor algebras and the differential geometry of arbitrary manifolds. *International Journal of Geometric Methods in Modern Physics* **4/7** (2007), 1117-1158. arXiv (03.3.2007 v1, 29.11.2007 v2)

- [141] 2007 (with V. V. FERNÁNDEZ, A. M. MOYA and E. A. NOTTE-CUELLO): Duality products of multivectors and multiforms, and extensors. *Algebras, Groups, and Geometries* **24**/1 (2007), 25-53. arXiv (18.3.2007)
- [142] 2007 (with V. V. FERNÁNDEZ, A. M. MOYA and E. A. NOTTE-CUELLO): Covariant derivatives of multivector and multiform fields. *Algebras, Groups, and Geometries* **24**/2 (2007), 221-235. arXiv (18.3.2007)
- [143] 2007 (with V. V. FERNÁNDEZ, A. M. MOYA and E. A. NOTTE-CUELLO): Covariant derivatives of extensor fields. *Algebras, Groups, and Geometries* **24**/3 (2007), 255-267. arXiv (18.3.2007)

- [144] 2007 (with Q. A. G. DE SOUZA): The hyperbolic Clifford algebra of multivectors. *Algebras, Groups, and Geometries* **24**/1 (2007), 1-23. arXiv (18.3.2007 v1, 31.3.2007 v2)
- [145] 2007 (with E. C. DE OLIVEIRA): *The many faces of Maxwell, Dirac and Einstein equations. A Clifford bundle approach*. Lecture Notes in Physics **722**. Springer, Berlin, 2007. XIV+445 p.
- [146] 2007 (with A. M. MOYA and V. V. FERNÁNDEZ): Multivector and extensor fields on smooth manifolds. *International Journal of Geometric Methods in Modern Physics* **4**/6 (2007), 965-985. arXiv (31.1.2005 v1, 29.11.2007 v5)

- [147] 2007 (with E. A. NOTTE-CUELLO and Q. A. G. DE SOUZA): The square of the Dirac and spin-Dirac operators on a Riemann-Cartan space(time). *Reports on Mathematical Physics* **60**/1 (2007), 135-157. arXiv (18.3.2007 v1, 29.11.2007 v2)
- [148] 2007 (with V. V. FERNÁNDEZ A. M. MOYA and R. DA ROCHA): Clifford and extensor calculus and the Riemann and Ricci extensor fields of deformed structures (M, ∇', η) and (M, ∇, g) . *International Journal of Geometric Methods in Modern Physics* **4**/7 (2007), 1159-1172. arXiv (31.1.2005 v1, 29.11.2007 v5)

- [149] 2007 (with Q. A. G. DE SOUZA and R. DA ROCHA): Conservation laws on Riemann-Cartan, Lorentzian and teleparallel spacetimes. I. The conservation laws. *Bulletin de la Société des Sciences et des Lettres de Łódź. Série: Recherches sur les Déformations* **52** (2007), 37-65. arXiv (3.5.2006 v1, 12.1.2008 v13)
- [150] 2007 (with Q. A. G. DE SOUZA and R. DA ROCHA): Conservation laws on Riemann-Cartan, Lorentzian and teleparallel spacetimes. II. Appendices: Clifford bundles, Maxwell theory, and teleparallel spacetimes. *Bulletin de la Société des Sciences et des Lettres de Łódź. Série: Recherches sur les Déformations* **52** (2007), 67-77.

- [151] 2007: Differential forms on Riemannian (Lorentzian) and Riemann-Cartan structures and some applications to physics. *Annales de la Fondation Louis de Broglie* **32**/4 (2007), 425-478. arXiv (19.12.2007 v1, 4.12.2008 v6)
- [152] 2008 (with E. A. NOTTE-CUELLO and R. DA ROCHA): The effective Lorentzian and teleparallel spacetimes generated by a free electromagnetic field. *Reports on Mathematical Physics* **62**/1 (2008), 69-89. arXiv (18.12.2006 v1, 03.1.2007 v3)
- [153] 2008 (with E. A. NOTTE-CUELLO): Superposition principle and the problem of additivity of the energies and momenta of distinct electromagnetic fields. *Reports on Mathematical Physics* **62**/1 (2008), 91-101. arXiv (12.12.2006 v1, 23.12.2006 v4)

- [154] 2008 (with R. DA ROCHA): Diffeomorphism invariance and local Lorentz invariance. *Advances in Applied Clifford Algebras* **18**/3-4 (2008), 945-961. arXiv (06.10.2006)
- [155] 2009 (with E. A. NOTTE-CUELLO): Freud's identity of differential geometry, the Einstein-Hilbert equations and the vexatious problem of the energy-momentum conservation in GR. *Advances in Applied Clifford Algebras* **19**/1 (2009), 113-145. arXiv (16.1.2008 v1, 5.3.2008 v4)
- [156] 2009 (with R. DA ROCHA): Reply to Itin, Obukhov and Hehl paper "An electric charge has no screw sense – a comment on the twist-free formulation of electrodynamics by da Rocha & Rodrigues". arXiv (10.12.2009). See also the comments in the Conclusions section of [157].

- [157] 2010 (with R. DA ROCHA): Pair and impair, even and odd form fields, and electromagnetism. *Annals of Physics* **19**/1-2 (2010), 6-34. arXiv (11.11.2008 v1, 13.8.2009 v7)
- [158] 2010 (with R. DA ROCHA): Rigorous formulation of duality in gravitational theories. *Journal of Physics A* **43**/20 (2010), 205206, 16 p.
- [159] 2010 (with R. DA ROCHA): Gauge fixing in the Maxwell like gravitational theory in Minkowski spacetime and in the equivalent Lorentzian spacetime. *AIP Conference Proceedings* **1316**, 466 (2010). arXiv (25.6.2008 v1, 12.12.2014 v6)
- [160] 2010 (with V. V. FERNÁNDEZ): *Gravitation as a plastic distortion of the Lorentz vacuum*. Fundamental Theories of Physics **168**. Springer, Heidelberg, 2010. x+153 p. arXiv.

- [161] 2010: Killing vector fields, Maxwell equations and Lorentzian spacetimes. *Advances in Applied Clifford Algebras* **20**/3-4 (2010), 871-884. arXiv (23.1.2008 v1, 13.8.2009 v5)
- [162] 2010 (with E. A. NOTTE-CUELLO & R. DA ROCHA): Some thoughts on geometries and on the nature of the gravitational field. *Journal of Physical Mathematics* **2** (2010), P100506, 21 p. Euclid. arXiv (14.7.2009)
- [163] 2011 (with E. C. DE OLIVEIRA and J. VAZ JR.): The mass spectrum of neutrinos. arXiv. (25.10.2011 v2)
- [164] 2011 (with E. C. DE OLIVEIRA and J. VAZ JR.): Superluminal Neutrinos from OPERA Experiment and Weyl Equation. arXiv. (10.10.2011)

- [165] 2011 (with J. F. T. GIGLIO): Riemann-Cartan connection and its decomposition. One more assessment of “ECE Theory”. arXiv (25.9.2011)
- [166] 2012 (with J. F. T. GIGLIO): Locally inertial reference frames in Lorentzian and Riemann-Cartan spacetimes. *Annals of Physics* **524**/5 (2012), 302-310. arXiv (11.11.2011 v2)
- [167] 2012 (with J. F. T. GIGLIO): Gravitation and electromagnetism as geometrical objects of a Riemann-Cartan spacetime structure. *Advances in Applied Clifford Algebras* **22**/3 (2012), 649-664. arXiv (24.9.2011 v1, 19.12.2011 v3)
- [168] 2012: Nature of the gravitational field and its legitimate energy-momentum tensor. *Reports on Mathematical Physics* **69**/2 (2012), 265–279. arXiv (24.9.2011 v1, 01.7.2012 v4)

- [169] 2012 (with E. C. DE OLIVEIRA): Extracting energy from an external magnetic field. arXiv (08.8.2012 v1, 20.9.2012 v2)
- [170] 2012 (with E. C. DE OLIVEIRA): Comment on "Self-interacting Elko dark matter with an axis of locality". *Physics Review D* **86** (2012), 128501.
- [171] 2012 (with F. G. RODRIGUES & R. DA ROCHA): The Maxwell and Navier-Stokes that follow from Einstein equation in a spacetime containing a Killing vector Field. *AIP Conference Proceedings* **1483** (2012), 277-295. arXiv (24.9.2011 v1, 6.10.2012 v6).
- [172] 2014 (with S. A. WAINER): A Clifford Bundle Approach to the Differential Geometry of Branes. *Advances in Applied Clifford Algebras* **24/3** (1014), 817-847. arXiv

- [173] 2014 (E. C. DE OLIVEIRA and J. VAZ JR.): A generalized electromagnetic theory for the mass spectrum of neutrinos. *Gravitation and Cosmology* **20**/1 (2014), 10-20.
- [174] 2014 (E. C. DE OLIVEIRA and J. VAZ JR.): Elko spinor fields and massive magnetic like monopoles. *International Journal of Theoretical Physics* **53**/12 (2014), 4381-4401. arXiv (19.6.2013)
- [175] 2015 (with E. A. NOTTE-CUELLO): Differential structure of the hyperbolic Clifford algebra. *Advances in Applied Clifford Algebras* **25**/1 (2015), 169-218. arXiv (13.3.2014)

- [176] 2016 (with S. A. WAINER, M. RIVERA-TAPIA, E. A. NOTTE-CUELLO and I. KONDRASHUK): A Clifford bundle approach to the wave equation of a spin 1/2 fermion in the de Sitter manifold. *Advances in Applied Clifford Algebras* **26**/1 (2016), 253-277. arXiv (19.2.2015 v1, 21.7.2015 v6)
- [177] 2016 (with E. C. DE OLIVEIRA): *The Many Faces of Maxwell, Dirac and Einstein Equations* (Second edition). *Lecture Notes in Physics* **992**, Springer, 2016. XVI+587 p.
- [178] 2016 (with S. A. WAINER): Notes on conservation laws, equations of motion of matter, and particle fields in Lorentzian and teleparallel de Sitter space-time structures. *Advances in Mathematical Physics* **2016**, Article ID 5465263, 27 p. arXiv (12.5.2015 v1, 23.11.2016 v2)

- [179] 2016 (with S. A. WAINER): Equations of motion and energy-momentum 1-forms for the coupled gravitational, Maxwell and Dirac fields. arXiv (19.1.2016 v1, 21.1.2016 v2)
- [180] 2016 (with S. A. WAINER): On the motion of a free particle in the DE SITTER manifold arXiv (21.01.2016)
- [181] 2016 (with S. A. WAINER): The relativistic HAMILTON-JACOBI equation for a massive, charged and spinning particle, its equivalent DIRAC equation and the DE BROGLIE-BOHM theory. arXiv (11.10.2016 v1, 23.2.2017 v2)
- [182] The Dirac-Hestenes equation and its relation with the relativistic DE BROGLIE-BOHM theory. arXiv (27.10.2016)
- [183] 2016: Bosonization of fermionic fields and fermionization of bosonic fields. arXiv (07.11.2016 v1, 15.11.2016 v2)

- [184] 2017 (with R. F. LEÃO and S. A. WAINER): Concept of Lie derivative of spinor fields a geometric motivated approach. *Advances in Applied Clifford Algebras* **27**/1 (2017), 209-227. arXiv (28.11.2014 v1, 30.11.2015 v3).
- [185] 2017 (with S. A. WAINER): Equations of motion and energy-momentum 1-forms for the coupled gravitational, Maxwell and Dirac fields. *Advances in Applied Clifford Algebras* **27**/1 (2017), 787-803.
- [186] 2017 (with J. VAZ JR.): Life in the Rindler Reference Frame: Does an Uniformly Accelerated Charge Radiate? Is there a Bell 'Paradox'? Is the Unruh Effect Real? arXiv (07.2.2017: To appear in a volume commemorating the 50th anniversary of IMEC)

[187] 2017: From the photon to Maxwell equation. Ponderations on the concept of photon localizability and photon trajectory in a DE BROGLIE-BOHM interpretation of quantum mechanics. arXiv (02.1.2017 v1, 23.2.2017 v2)