

# Exercise Sheet 5

## Multivariate Calculus

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Friday, April 23rd, 2021

*The exercises must be handed in on Blackboard on Monday, May 10th at the latest.*

### Problem 1 (10 points)

For each of the following integrals, change the order of integration and compute the integral. It might be helpful for you to draw the domain of integration:

1. (5 points)

$$\int_0^{\sqrt{2}} \int_{-\sqrt{4-2y^2}}^{\sqrt{4-2y^2}} y dx dy$$

2. (5 points)

$$\int_0^4 \int_{\frac{y}{2}}^{\sqrt{y}} x^2 y^2 dx dy$$

### Problem 2 (6 points)

Let  $D$  be the region of the first quadrant of  $\mathbb{R}^2$  limited by the lines  $y = 0$  and  $3x - 4y = 0$  and the circumference  $x^2 + y^2 = 25$ . Express the integral

$$\iint_D x dx dy$$

as an iterated integral and compute it.

### Problem 3 (4 points)

Compute the area of the region  $D = \{(x, y) \in \mathbb{R}^2 \mid 3y \geq x^2, x^2 + y^2 \leq 4\}$ .