

985-05-162

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The most natural convexities in a graph $G = (V, E)$ are path convexities defined by a system \mathcal{P} of paths in G that contain all geodesics. The canonical choices for \mathcal{P} are provided by selecting all paths, triangle paths, minimal paths and geodesics. The standard convexity is the geodesic convexity in which a vertex set S is said to be (geodesically) convex if $S = I[S]$, where $I[S]$ (called the geodesic closure of S) is the set of all shortest $x - y$ paths (also called geodesics) for every $x, y \in S$. A set of vertices is called geodesic if $I[S] = V$, and it is said to be a hull set if $[S] = V$, where $[S]$ (called the convex hull of S) is the smallest convex set containing S . Certainly, every geodesic set is a hull set. Given a vertex set W , a Steiner W -tree is a tree containing W , of minimum order. Moreover, W is called an Steiner set if $S(W) = V$, where $S(W)$ (called the Steiner interval of W) is the collection of all vertices of G which lies on some Steiner W -tree. Contrarily to what was stated in a recent published paper [Disc. Math. 242 (2002), no. 1-3, 41–54.] we have proved that not every Steiner set is a geodesic set. Going one step further, we have approached the following question: Is every Steiner set a Hull set?

(Received February 07, 2003)